



Risk Spillovers among Financial Institutions

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The views expressed in this paper are those of the authors and do not necessarily represent those of the Federal Reserve Bank of New York or the Federal Reserve System

[Motivation]

- “Risk spillovers” across financial institutions
 - Commercial banks, Investment banks, Hedge fund styles
- Why do risk spillovers matter?
 - Financial stability Central banks
 - Counterparty credit risk management Dealers and banks
 - Portfolio management Fund-of-Funds
- Risk spillovers in crisis:
 - 87 crash, Asian financial crisis, LTCM crisis, Bear Stearns crisis

[Measuring Risk Spillovers]

- Our proposal: **CoVaR**
- VaR conditional that others are in distress
- CoVaR is based on quantile regressions
 - Focus on tails
 - Data efficient
 - Simple

[Overview]

1. Quantile regressions – refresher
2. Spillover risk – CoVaR
3. Offloading spillover risk with factors
4. Incentives to offload

Quantile Regressions – A Refresher

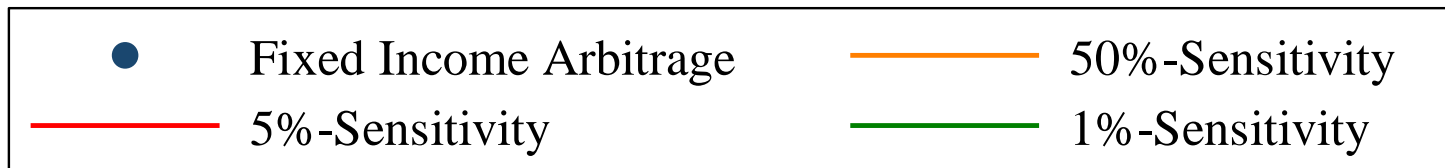
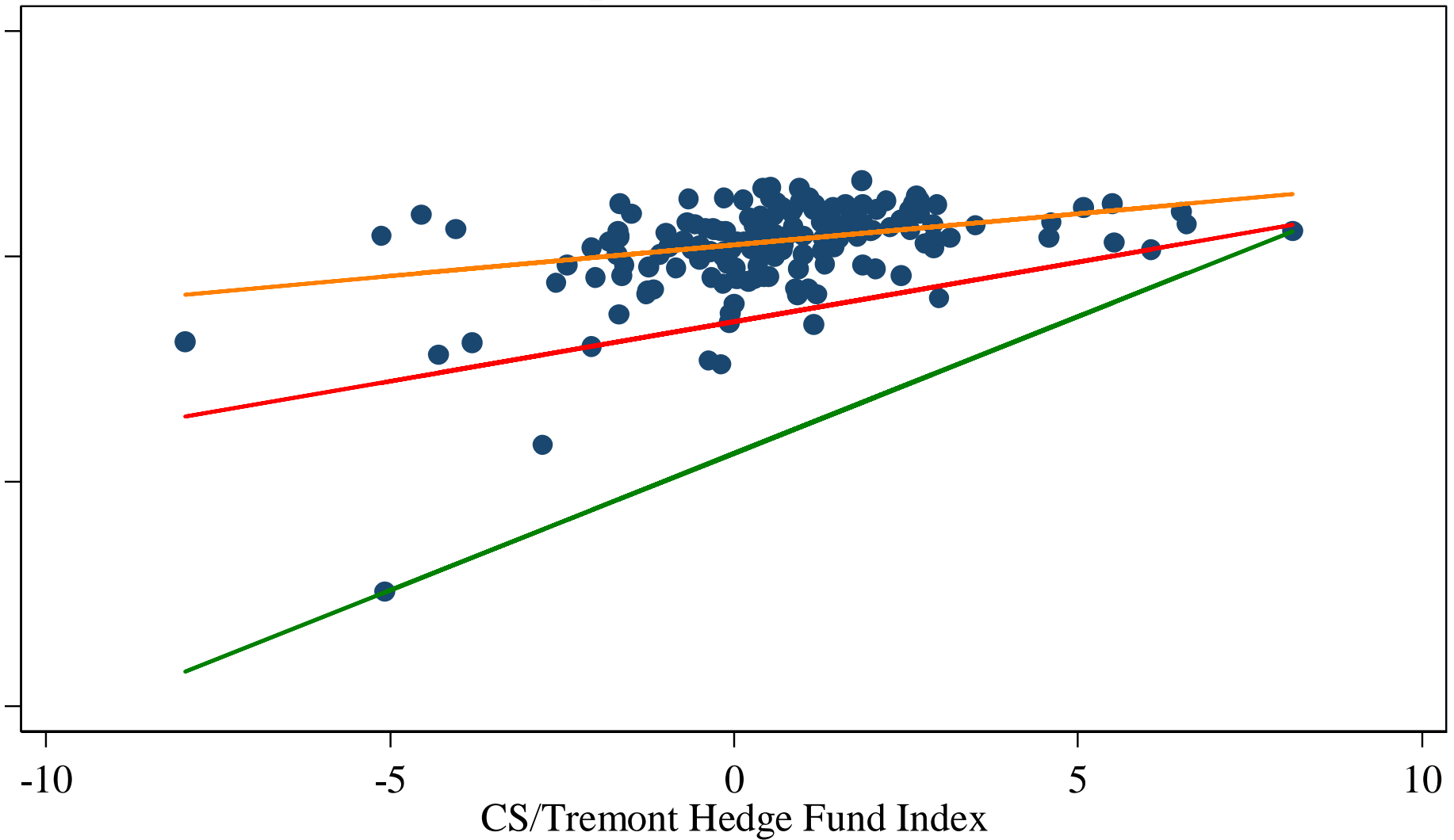
- **OLS regression:** min sum of squared residuals:

$$\beta^{OLS} = \arg \min_{\beta} \sum_t (y_t - \alpha - \beta x_t)^2$$

- **Quantile regression:** min weighted absolute values:

$$\beta^q = \arg \min_{\beta} \sum_t \begin{cases} q |y_t - \alpha - \beta x_t| & \text{if } y_t - \alpha - \beta x_t \geq 0 \\ 1 - q |y_t - \alpha - \beta x_t| & \text{if } y_t - \alpha - \beta x_t < 0 \end{cases}$$

q-Sensitivities



Quantiles and Value-at-Risk

- Quantile regressions give an estimate of the quantile q of y as a linear function of x :

$$\hat{y}_q | x = F_y^{-1}(q | x) = \alpha_q + \beta_q x$$

where $F^{-1}(q|x)$ is the inverse CDF conditional on x .

- So $F^{-1}(q|x) = q\%$ Value-at-Risk conditional on x .

Note our sign convention!

CoVaR – measure of risk spillover


- Return R^i depends on return R^j for quantile q :

$$\hat{R}_q^i = \hat{\alpha}_q^{ij} + \hat{\beta}_q^{ij} R^j$$

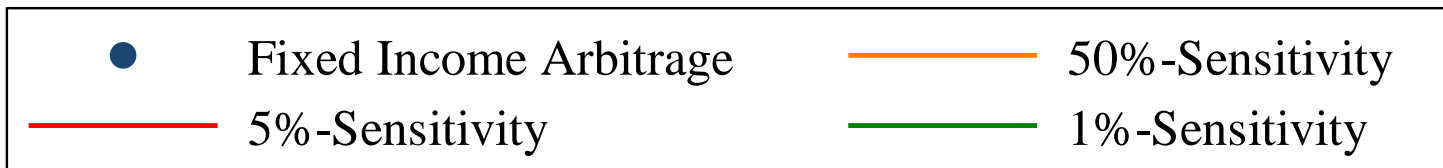
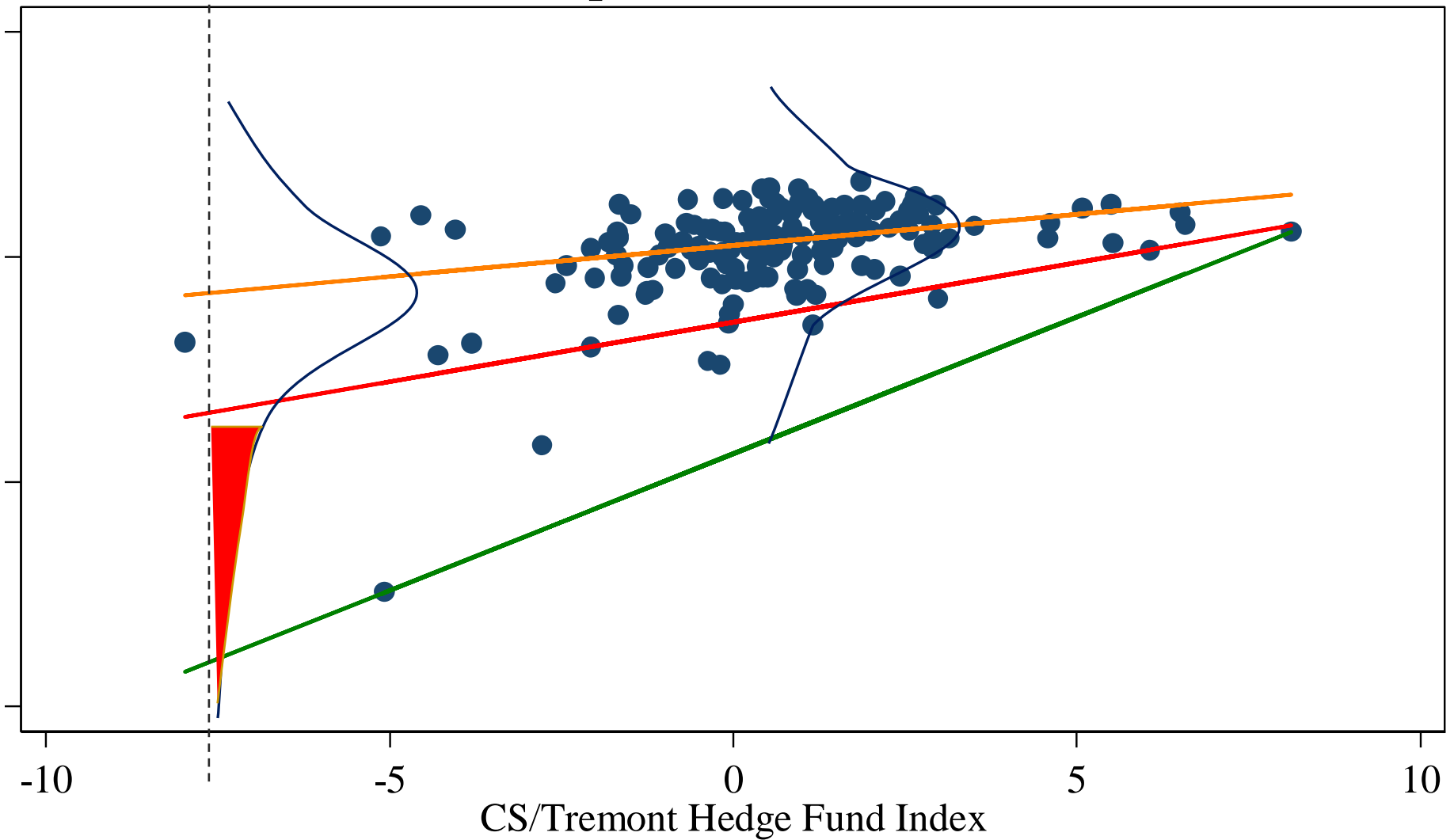
- Definition:** We denote the **CoVaR^{ij}**, the VaR of style i conditional on the (unconditional) VaR of style j by:

$$CoVaR_q^{ij} = VaR_q^i | VaR_q^j = \hat{\alpha}_q^{ij} + \hat{\beta}_q^{ij} VaR^j$$

- Conditioning shifts

- mean  contagion effect
- variance
 - lower
 - increase due to heteroskedasticity + tail behavior

q-Sensitivities



[Data]

- CRSP equity returns 1986/4-2008/3
 - Five commercial banks
 - Bank of America, Citibank, J. P. Morgan Chase, Wachovia, Wells Fargo
 - Five investment banks
 - Bear Stearns, Goldman Sachs, Lehman Brothers, Merrill Lynch, Morgan Stanley

- CSFB/Tremont hedge fund strategies 1994/1-2008/05
 - Long/Short Equity, Global Macro, Event Driven, Fixed Income Arbitrage, Multi-Strategy, Emerging Markets, Equity Market Neutral, Convertible Arbitrage, Managed Futures, Dedicated Short Bias

- Commercial bank and security broker dealer industry portfolios from Ken French 1926/7-2007/3

Result 1a: CoVaRs > VaR

	<u>5%-VaR</u>	<u>5%-CoVaR / 5%-VaR</u>				t-stats		
		percent increase				CB	IB	HF
Panel A: Institutions		CB	IB	HF		CB	IB	HF
Commercial Banks (CB)	-12.23	43	29	18	-12.85	5.01	3.73	0.94
Investment Banks (IB)	-13.69	45	24	61	-7.86	5.03	3.14	4.13
Ten Hedge Fund Styles (HF)	-2.40	27	23	48	-9.24	1.40	1.13	2.84

	<u>5%-VaR</u>	<u>5%-CoVaR / 5%-VaR</u>				t-stats		
		percent increase				CB	IB	HF
Panel B: Portfolios 1926-2008		CB	IB	HF		CB	IB	HF
Commercial Bank Portfolio (CB)	-10.13	.	42.64	.	-17.84	.	6.15	.
Security Broker Dealer Portfolio (IB)	-11.83	37.44	.	.	-17.37	5.06	.	.

Result 1b: Quantile-CoVaRs > OLS-CoVaRs

	<u>5%-CoVaR / OLS-CoVaR</u>			t-stats		
	percent increase			CB	IB	HF
Panel A: Institutions	CB	IB	HF	CB	IB	HF
Commercial Banks (CB)	18	4	10	2.64	0.53	0.71
Investment Banks (IB)	15	12	32	1.91	1.83	2.57
CSFB/Tremont Hedge Fund Styles (HF)	21	17	34	1.22	0.99	2.48
	<u>5%-CoVaR / OLS-CoVaR</u>			t-stats		
	percent increase			CB	IB	
Panel B: Portfolios 1926-2008	CB	IB		CB	IB	
Commercial Bank Portfolio (CB)	.	16		.	2.29	
Security Broker Dealer Portfolio (IB)	11	.		1.35	.	

Result 2: HF-VaR predict I-Bank's-CoVaR

	<u>5%-VaR</u>	<u>5%-CoVaR / 5%-VaR</u> percent increase				t-stats		
Panel A: Institutions		CB	IB	HF		CB	IB	HF
Commercial Banks (CB)	-13.90	-3	-2	-16	-8.58	-0.61	-0.17	-1.02
Investment Banks (IB)	-15.09	4	5	32	-4.27	0.49	0.68	2.83
Ten Hedge Fund Styles (HF)	-3.30	-2	2	3	-6.57	-0.28	0.23	0.41

	<u>5%-VaR</u>	<u>5%-CoVaR / 5%-VaR</u> percent increase			t-stats	
Panel B: Portfolios 1926-2008		CB	IB		CB	IB
Commercial Bank Portfolio (CB)	-11.49	.	4	-11.00	.	0.72
Security Broker Dealer Portfolio (IB)	-13.78	-7	.	-12.16	-1.61	.

[Overview]

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6-Risk Factor Pricing Model

Factors:

- Repo - 3 Month Treasury :
- 10 Year - 3 Month Treasury Return:
- Moody's BAA - 10 Year Treasury Return:
- CRSP Market Excess Return:
- VIX Straddle Excess Return:
- Variance Swap Return:

Interpretation:

- “Flight to Quality”*
- “Business Cycle”*
- “Credit Indicator”*
- “Equity Market Risk”*
- “Volatility Exposure”*
- “Variation in Price of Risk”*

Offloaded Returns

- All factors are excess returns
 - We can offload systematic risk
 - CoVaR of offloaded returns

- Offloaded Return $i = R^i - \beta_q^i X = \alpha_q^i + res_q^i$

[Result 3a: 5%-offloaded returns CoVaRs ~ VaRs]

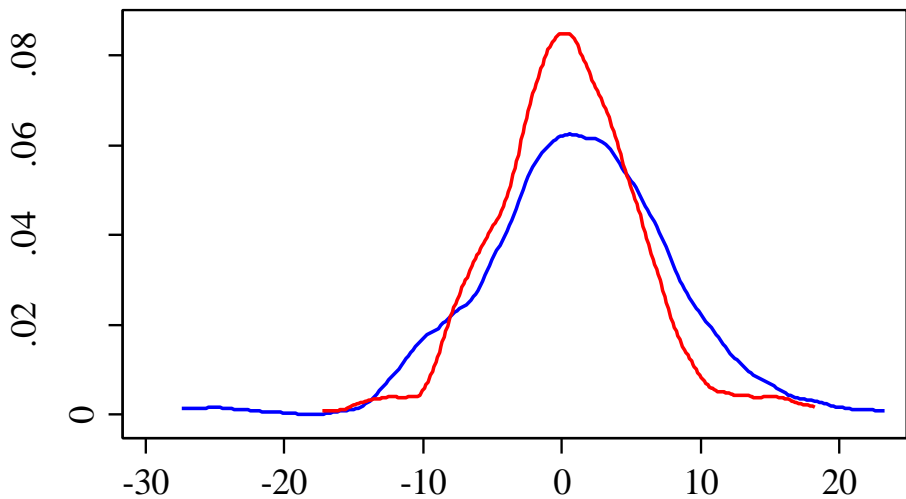
	<u>5%-VaR</u>	<u>5%-CoVaR / 5%-VaR</u>				t-stats		
		percent increase				CB	IB	HF
		CB	IB	HF		CB	IB	HF
Commercial Banks (CB)	-7.86	30	3	-8	-33.45	3.54	0.31	-0.93
Investment Banks (IB)	-10.28	3	14	0	-60.95	0.39	1.76	-0.03
Ten Hedge Fund Styles (HF)	-2.36	1	1	10	-35.25	0.14	0.08	1.61

Result 3b: Offloaded Returns: Quantile CoVaRs ~ OLS VaRs

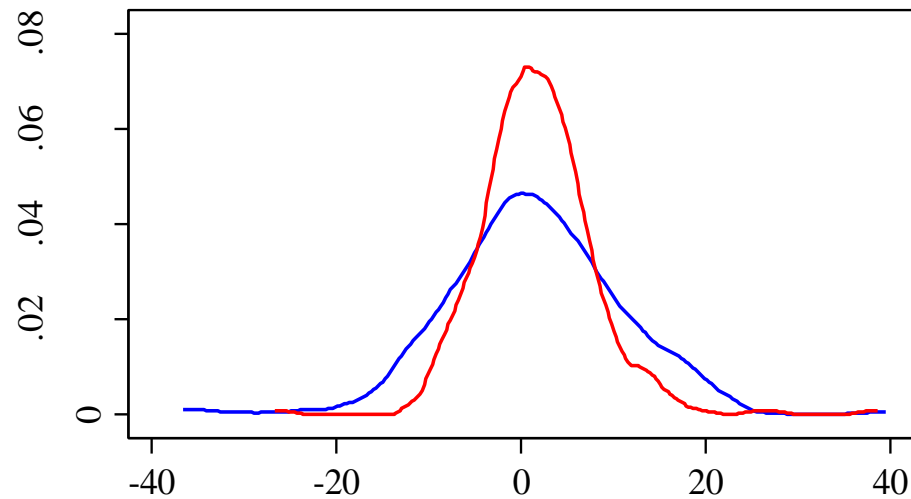
	<u>5%-CoVaR / OLS-CoVaR</u>			t-stats		
	percent increase			CB	IB	HF
	CB	IB	HF	CB	IB	HF
Commercial Banks (CB)	-7	-20	-2	-0.92	-2.80	-0.11
Investment Banks (IB)	-14	1	-1	-1.14	0.10	-0.07
CSFB/Tremont Hedge Fund Styles (HF)	3	2	-2	0.33	0.20	-0.20

Figure 1: Kernel Densities of Total and 5%-Offloaded Returns

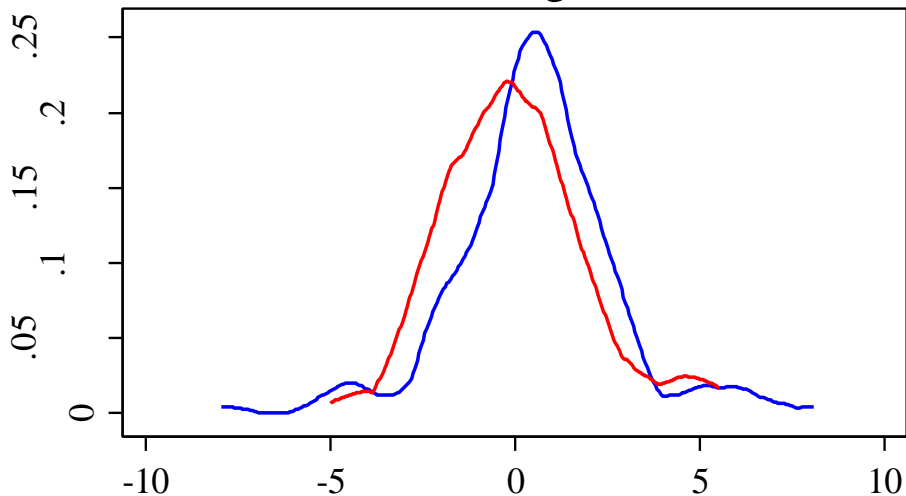
Commercial Banks



Investment Banks



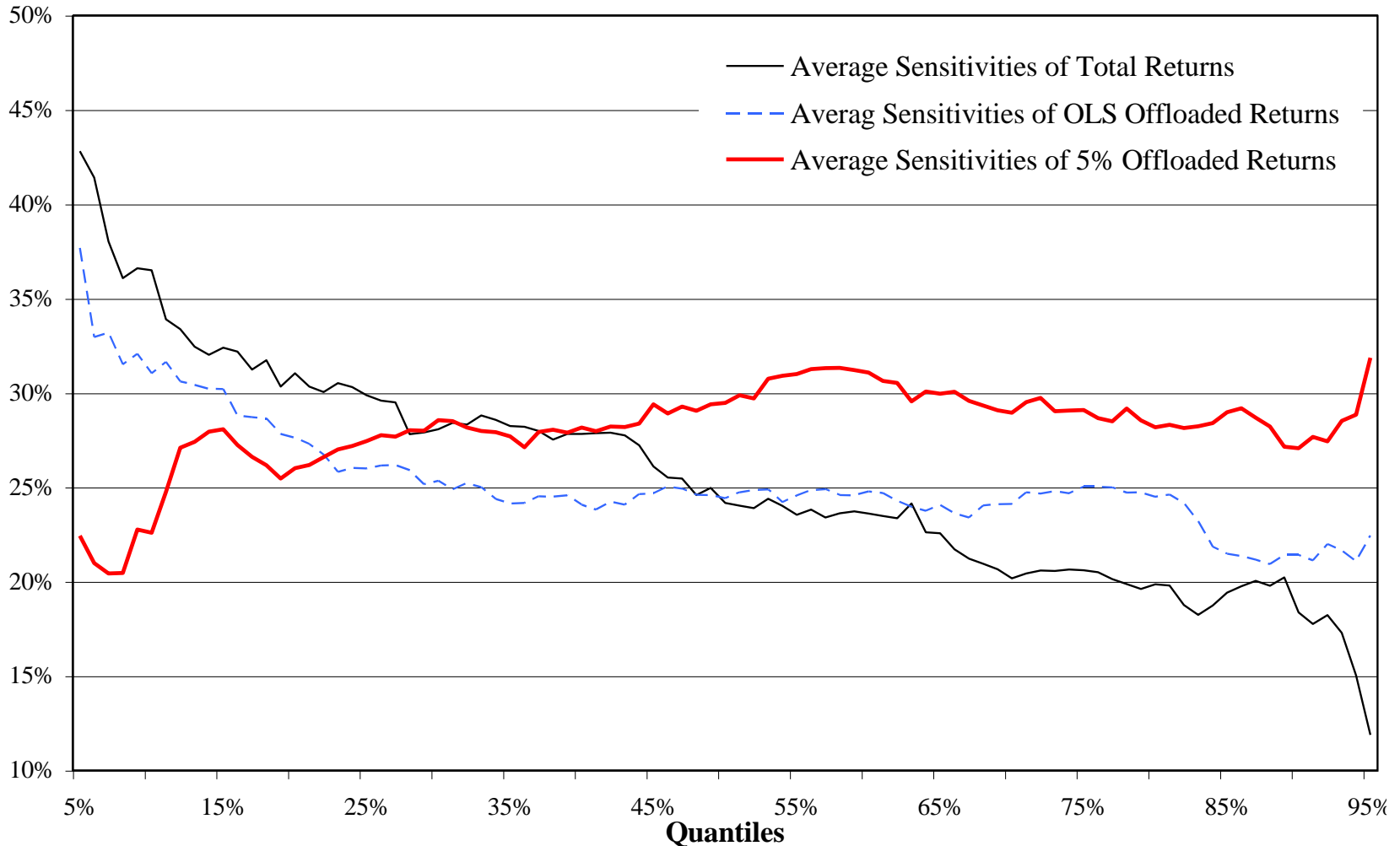
CS/Tremont Hedge Fund Index



- Hedging reduces left tail
- But average returns decrease
- Incentives to hedge spillover risk

q-Sensitivities: Total and Offloaded Returns

Figure 2: Average q-Sensitivities by Quantiles



[Related Literature]

- **Dependence / contagion:**

Boyson, Stahel, Stulz (2008), Chan, Getmansky, Haas, Lo (2006), Adrian (2007), Forbes, Rigobon (2002)

- **Hedge fund tail risk:**

Asness, Krail, Liew (2001), Agarwal & Naik (2004), Bali, Gokcan, Liang (2007), Liang & Park (2007), Bondarenko (2004)

- **Pricing factors:**

Fung and Hsieh (2001, 2002, 2003), Hasanhodzic & Lo (2007)

- **Finance applications of quantile regressions:**

Bassett and Chen (2001), Chernozhukov and Umantsev (2001)

Summary

- Institutions have incentives to hold tail risk
 - Holding tail risk increases returns
- There is spillover of tail risk among hedge funds and among banks, as well as between hedge funds and banks (contemporaneous and lagged)
- The increase in *CoVaR* relative to *VaR* can be offloaded with **liquid, tradable** risk factors

[Robustness Analysis]

- Alternative measure of tail risk:
1%-CoVaR and Expected Shortfall
- Alternative measure of sensitivities:
GARCH variances

Robustness check: 1%-CoVaR and Expected shortfall

	<u>1%-VaR</u>	<u>1%-CoVaR / 1%-VaR</u> percent increase		t-stats	
		CB	IB	CB	IB
Panel A: 1%-CoVaR					
Commercial Bank Portfolio (CB)	-21.46	.	23	-9.06	1.89
Security Broker Dealer Portfolio (IB)	-22.46	38	.	-9.30	3.44
	<u>5%-ES</u>	<u>5%-CoES / 5%-ES</u> percent increase		t-stats	
		CB	IB	CB	IB
Panel B: 5%-Expected Shortfall					
Commercial Bank Portfolio (CB)	-13.67	.	40	-13.98	6.74
Security Broker Dealer Portfolio (IB)	-16.01	37	.	-14.63	5.95

Figure 3: Average GARCH Covariances over Time

