



# THE I-THEORY OF MONEY

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Updates: [http://www.princeton.edu/~markus/research/papers/i\\_theory\\_slides.pdf](http://www.princeton.edu/~markus/research/papers/i_theory_slides.pdf)

# || Motivation

- Main features
  - Model that combines money and intermediation – inside money
  - Value of money is endogenously determined
    - (Samuelson, Bewley, KM, ...)
  - Fisher (1933) deflationary spiral
    - Negative shock hits assets side of intermediaries' balance sheets and is amplified through leverage and volatility dynamics
    - Decline in inside money, leads to deflationary pressure hits intermediaries' balance sheet on the liability side
  - Inside money and outside money
    - "Endogenous" money multiplier =  $f(\text{health of intermediary sector})$
  - Monetary policy
    - Redistribution from/towards intermediary sector
      - Difference to New Keynesian framework
    - "Greenspan put" - time-inconsistency
      - Difference to example in Kydland-Precott
  - Unified framework to study financial and monetary stability

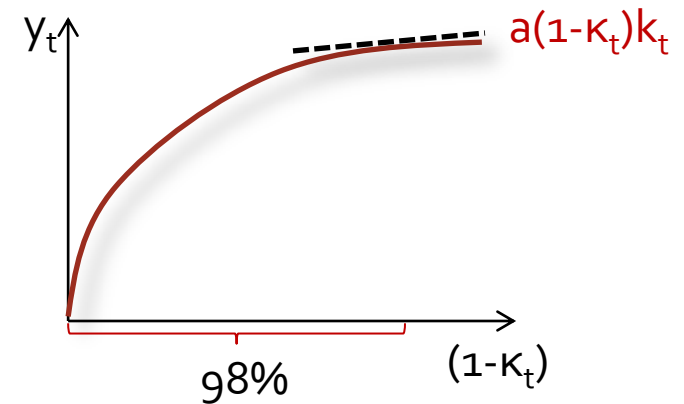
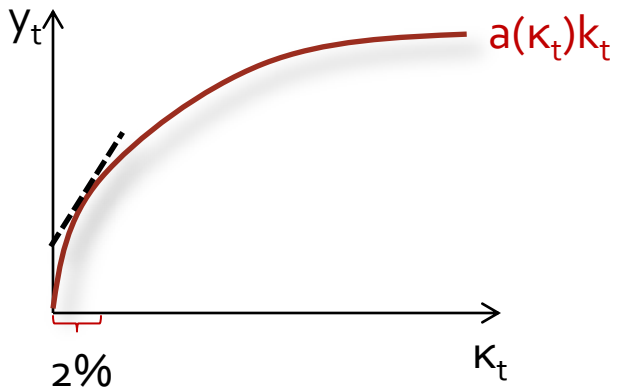
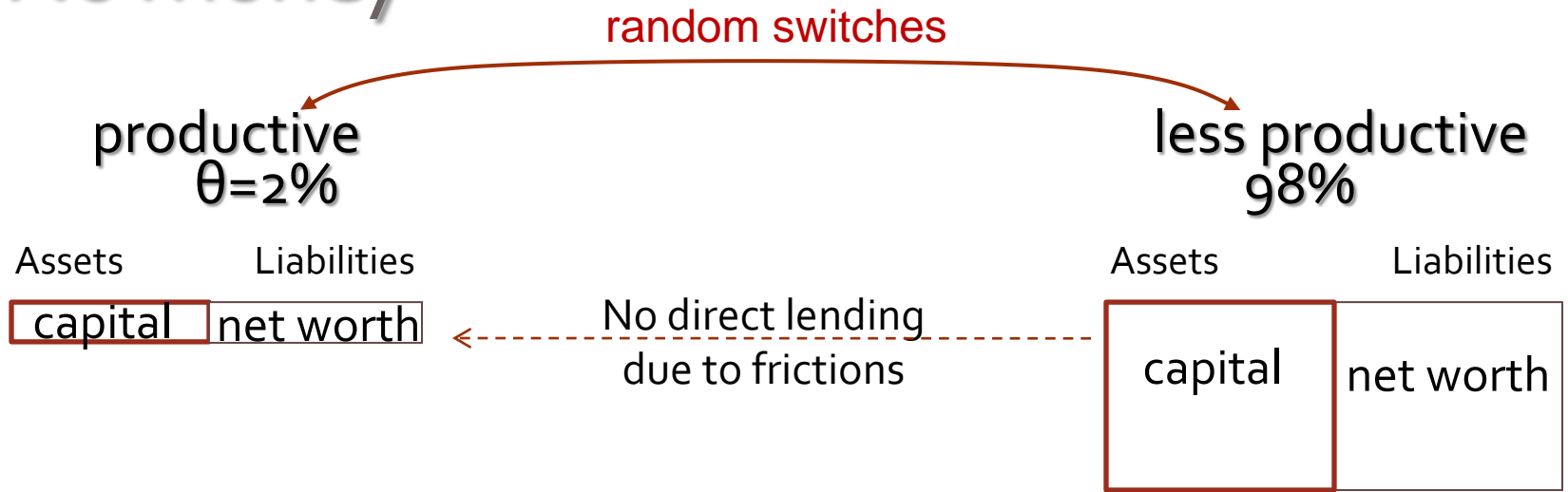
# || Motivation – some stylized facts/empirics

- Stylized facts from current crisis
  - Deflationary pressure
  - Money multiplier collapsed (see e.g. Goodhart 2010)
    - Monetary base increased
    - M<sub>3</sub> stayed roughly constant
  - Banking sector profits were helped by monetary economics
  - Aggressive risk-taking before crisis
- Empirical findings
  - King- Ploser (1984) inside money has significantly more power for output than monetary base
  - Mervin King (1994) more indebted countries suffered sharper downturn in 1990s recession
  - Eisfeld-Rampini (2008) less capital reallocation in downturns

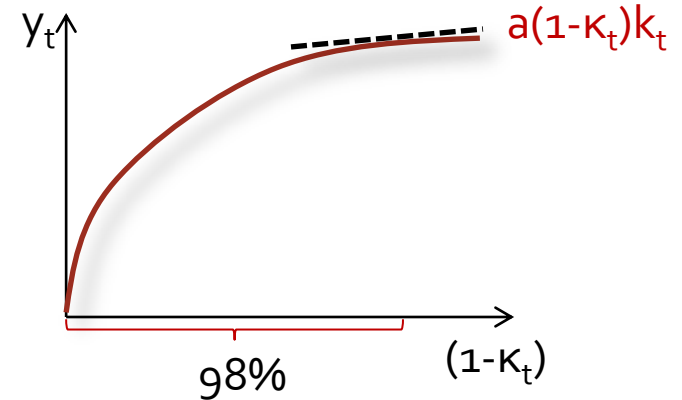
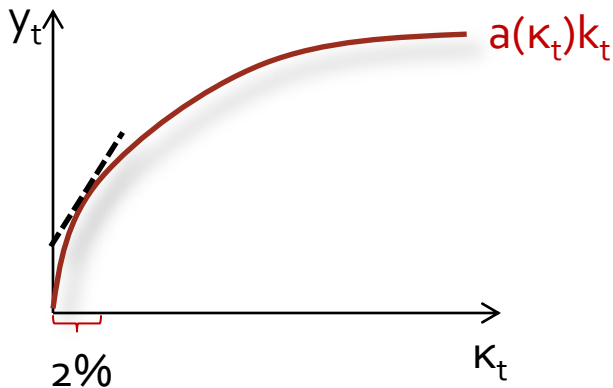
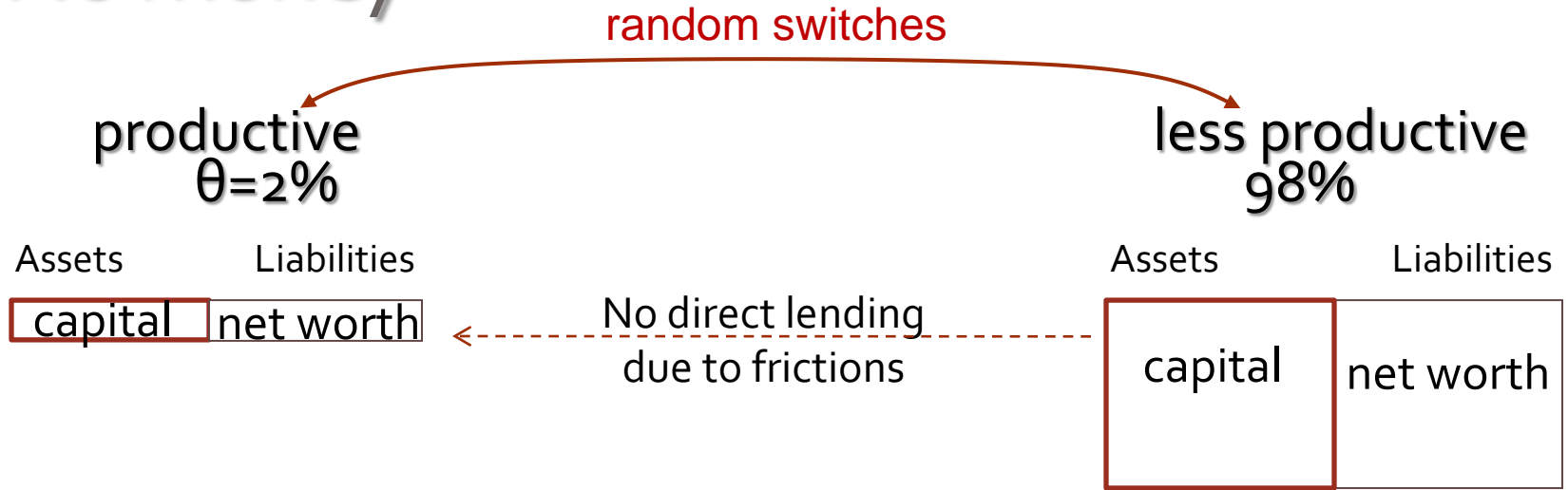
# || Roadmap

- Passive monetary policy - “Gold standard”
  - No money, no lending
  - Outside money (Polar case 1)
  - Perfect lending (Polar case 2)
  - Lending through intermediated lending (inside money)
    - Lending and money multiplier depends on net worth of i-sector
    - Deflation spiral
- Active Monetary Policy
  - Introduce long-term bond and OMO
  - Redistributive effects
  - “Greenspan put” - Time-inconsistency
- Differences to New Keynesian framework

# || No money



# No money

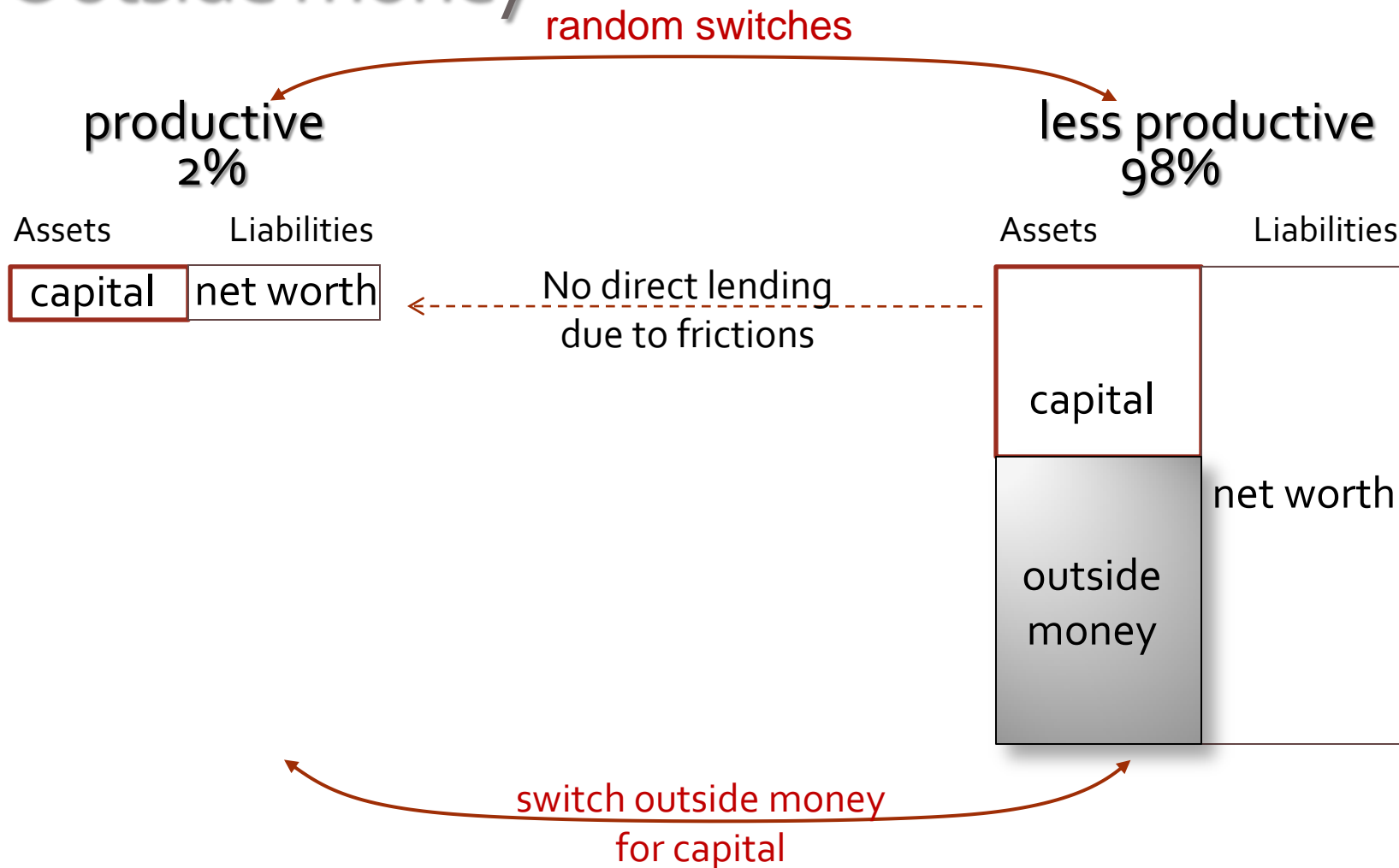


sector shock  
(exogenous risk)

- $dk_t = (\phi(i_t) - \delta) k_t dt + \sigma k_t dZ_t$

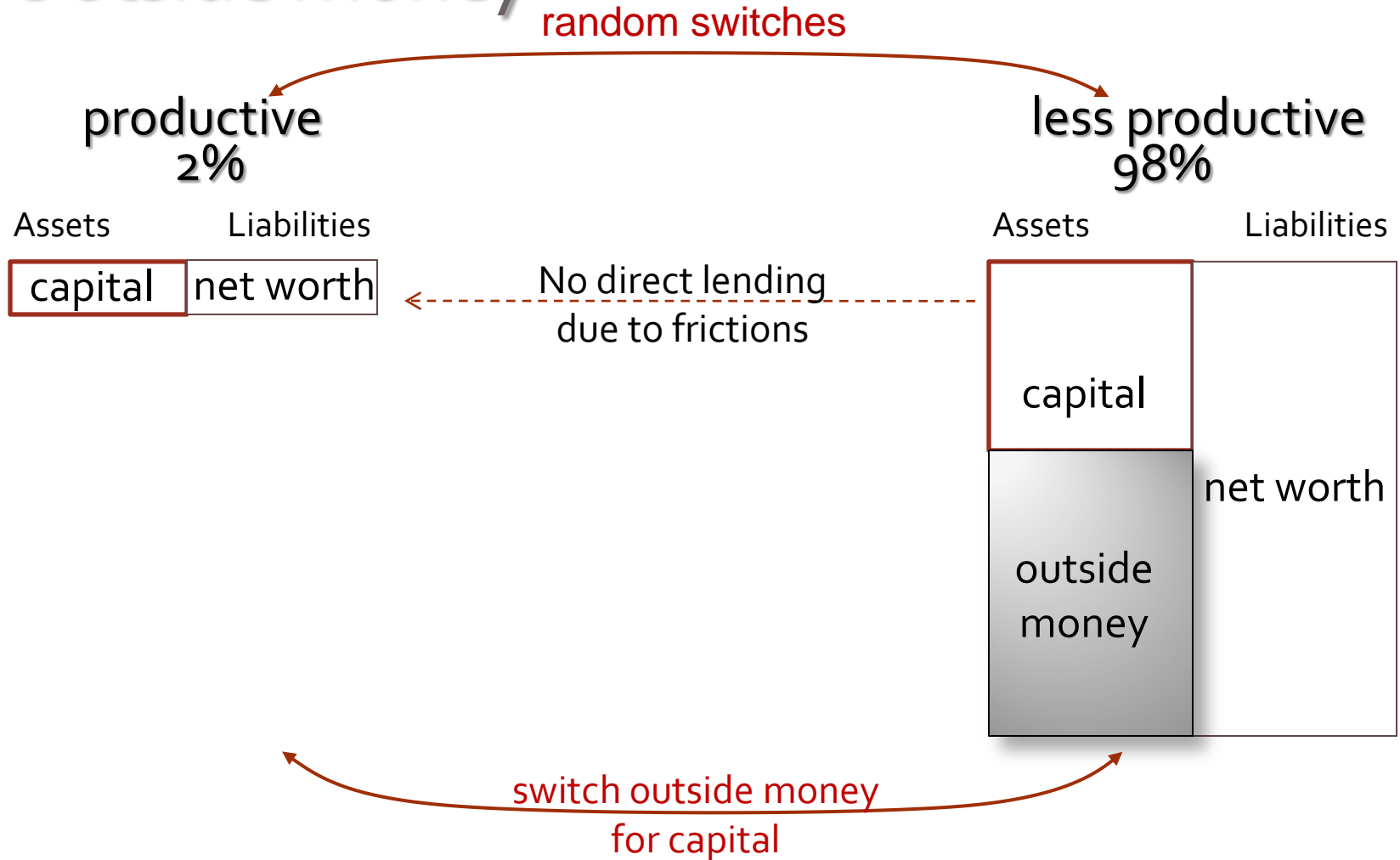
$dZ_t=0$

# Outside money



- More capital is in “productive hands”
- Notice difference to Bewley economy
  - Productivity shocks vs. endowment shocks

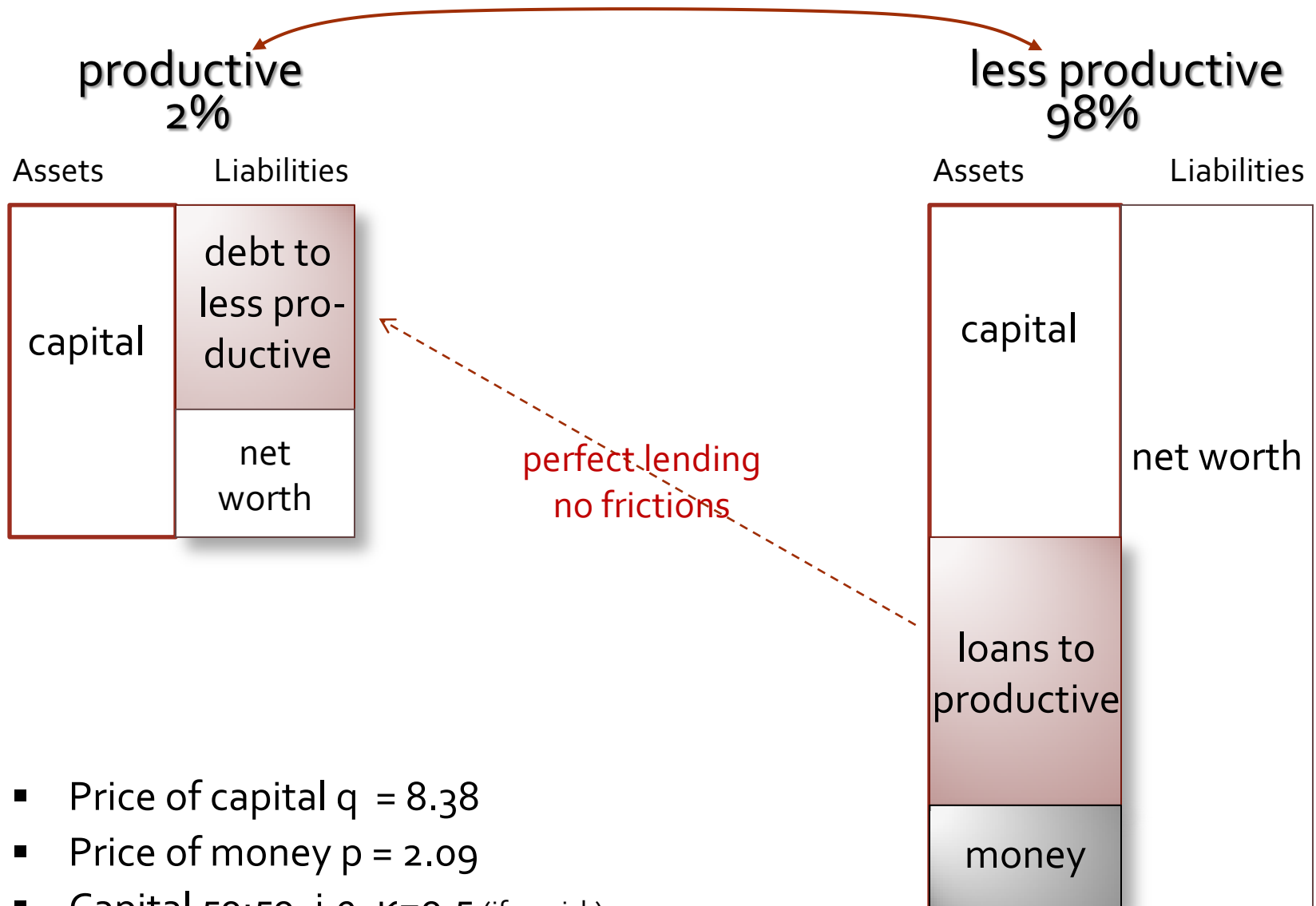
# Outside money



- Price of capital:  $q = 7.84$
- Price of money:  $p = 7.04$
- Fraction of capital held by productive HH:  $\pi = 4.2 \%$



# Other polar case: Unconstrained borrowing

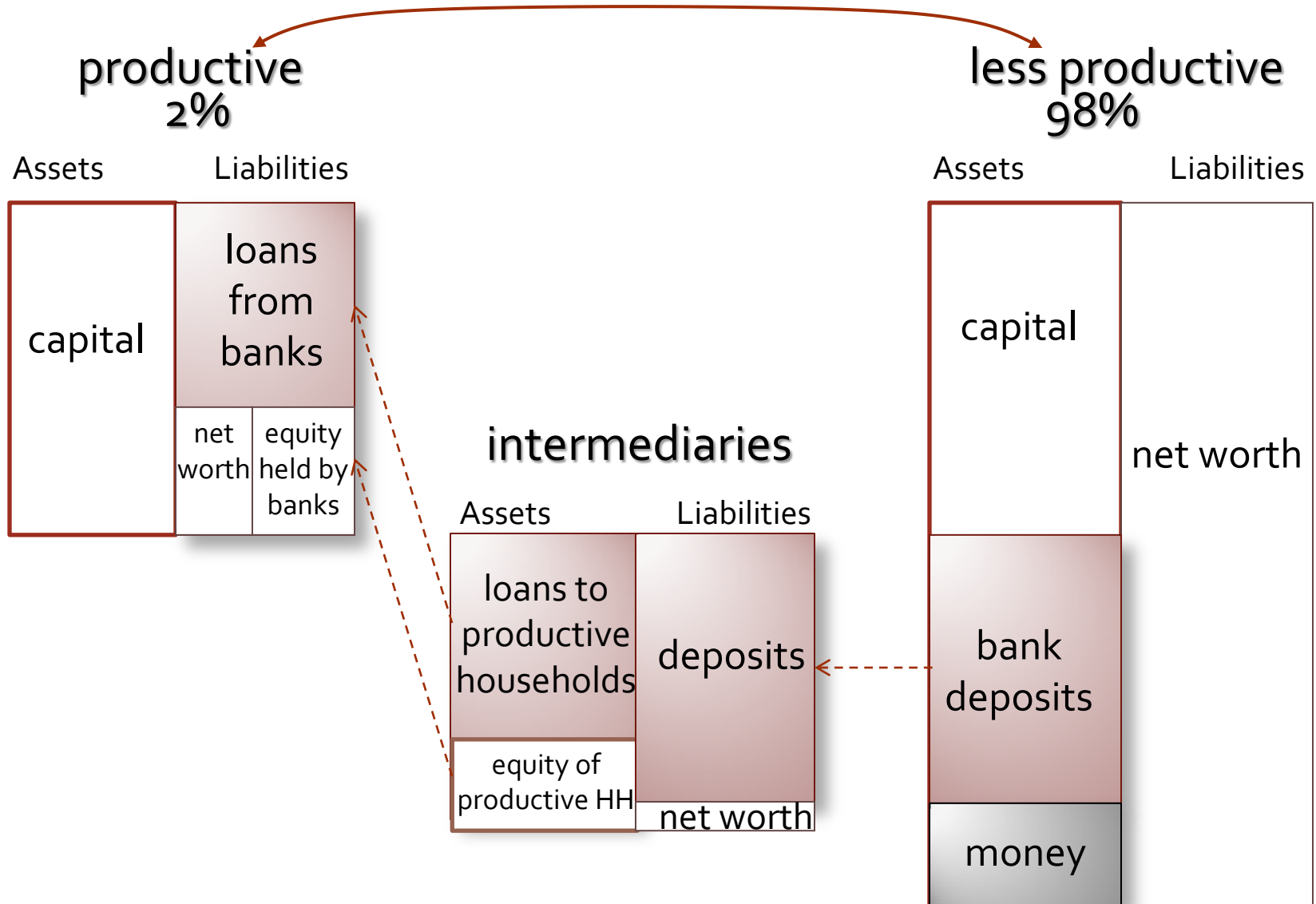


- Price of capital  $q = 8.38$
- Price of money  $p = 2.09$
- Capital 50:50, i.e.  $\kappa=0.5$  (if no risk)

# Compare

- With borrowing:  $q = 8.38, p = 2.09$
- Without borrowing:  $q = 7.84, p = 7.04$ 
  - capital allocated inefficiently – productive agents hold only 4.2%
  - underinvestment, as the price of capital  $q$  is depressed
  - total net worth of living agents (measured in current output) is actually greater, but investments generate lower return

# Intermediaries



# Intermediaries

productive  
2%

less productive  
98%

Assets	Liabilities	
capital	loans from banks	
	<table border="1"> <tr> <td>net worth</td> <td>equity held by banks</td> </tr> </table>	net worth
net worth	equity held by banks	

$\alpha$

## intermediaries

Assets	Liabilities
loans to productive households	deposits
equity of productive HH	

Assets	Liabilities
capital	net worth
bank deposits	
money	

assume that bank is exposed to a fraction  $\geq \alpha$  of risk of capital it finances "skin in the game"

# || The big picture

- Intermediaries net worth
  - Zero: like economy with only outside money (p high)
  - Very large: perfect lending (no frictions) (p low)
  - Intermediate: amplification – (non-linear effects)  
money multiplier changes  
outside money stays constant, inside money fluctuates
- Contracting friction:
  - Intermediaries have to hold  $\alpha$  fraction of risk  
(in order to have incentive to monitor)
  - No contracting on productivity switch – relation to Bewley
  - (no distinction between cash flow news,  $k_t$ , and SDF news)

# Endogenous risk - amplification

- Exogenous risk: cash flow news/shock on k

$$dk_t = (\phi(i_t) - \delta) k_t dt + \sigma k_t dZ_t$$

- Endogenous risk: SDF news

- Price of capital (in terms of output)

$$dq_t = \mu_t^q q_t dt + \sigma_t^q q_t dZ_t$$

Endogenous, fluctuating between 7.04 and 8.38, depending on the amount of lending/bank net worth

- Asset side of HH:  $d(k_t q_t) = \dots + (\sigma_t^q + \sigma) (k_t q_t) dZ_t$

□

▪

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# Endogenous risk - amplification

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Endogenous, fluctuating between 7.04 and 8.38, depending on the amount of lending/bank net worth

- Asset side of HH:  $d(k_t q_t) = \dots + (\sigma_t^q + \sigma) (k_t q_t) dZ_t$

- Price of money (aggregate value of money is  $p_t K_t$ )

$$dp_t = \mu_t^p p_t dt + \sigma_t^p p_t dZ_t$$

endogenous, fluctuating between 2.09 and 7.84

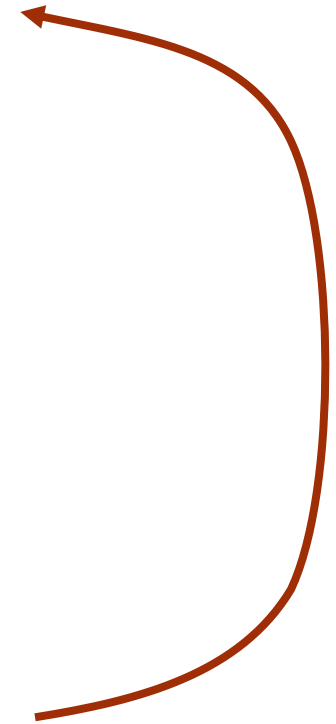
- Money risk:  $d(p_t K_t) = \dots (p_t K_t) dt + (\sigma_t^p + \pi_t \sigma) (p_t K_t) dZ_t$

- Bank risk:  $n_t (\sigma_t^p + \pi_t \sigma) + x_t (\sigma_t^q + \sigma - \sigma_t^p - \pi_t \sigma)$

intermediaries will charge a fee  $x_t f_t$  for taking on this risk

# Amplification through “deflation spiral”

- As intermediaries' net worth declines
- Intermediation + *inside money* shrinks
  - Economic activity declines
- Value of *outside money* rises - deflation
- Intermediaries are doubly hit
  - Asset side: asset values decrease
  - Liability side: real debt value increases
- Deflationary spiral





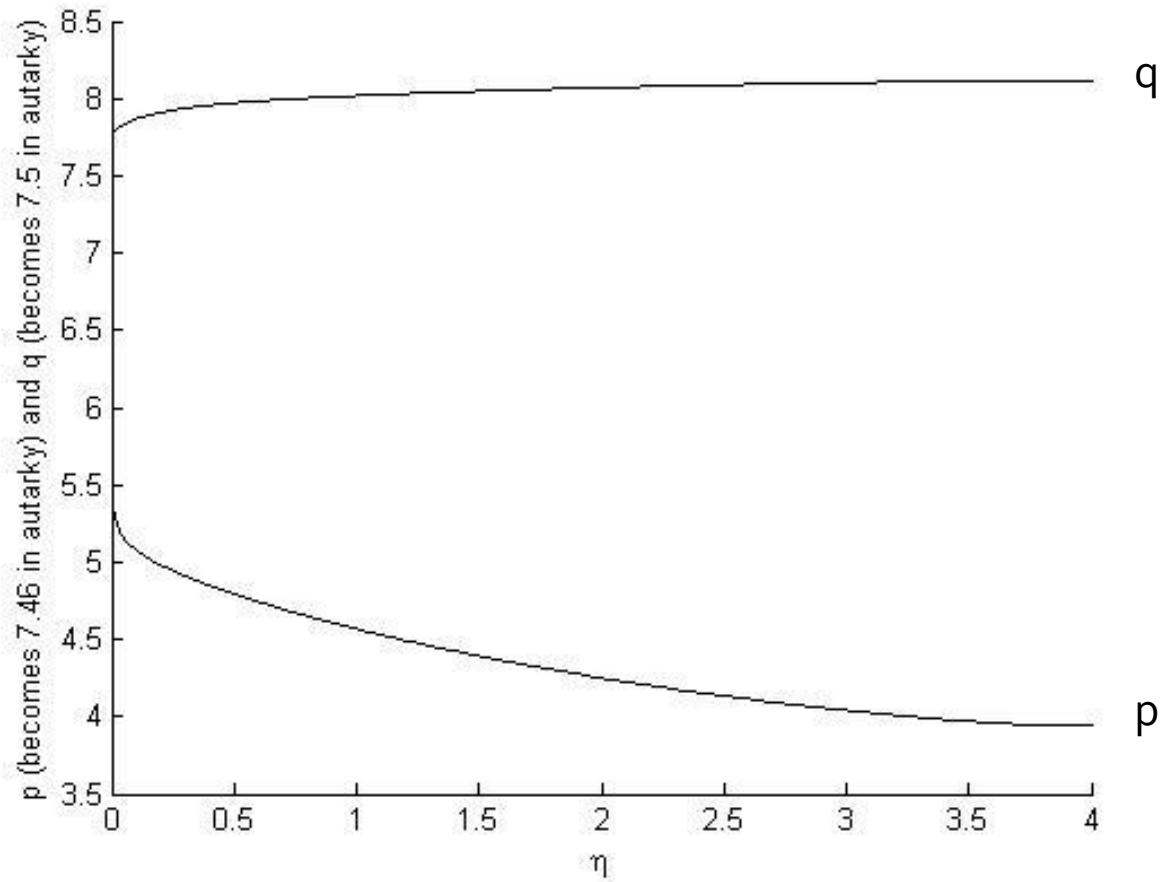
# Equilibrium definition

- An equilibrium consists of functions that for each history of macro shocks  $\{Z_s, s \in [0, t]\}$  specify
  - the price of capital  $q_t$ , the value of money  $p_t$  and bank fees  $f_t$
  - capital holdings  $\pi_t$  and  $1 - \pi_t$  and rates of investment of productive and unproductive households
  - rates of consumption of productive and unproductive households
  - such that
    - given prices and bank fees, productive households choose asset holdings, consumption and investment to maximize utility
    - given fees, banks lend and consume to maximize utility
    - unproductive households - portfolio of capital and money/deposits
    - markets for capital, output and loans clear

# Scale invariance

- Our model is scale invariant in
  - $N_t$  (total intermediary net worth) and
  - $K_t$  (aggregate capital)
- $\eta_t = N_t/K_t$
- Solve for
  - $\pi_t$  = fraction of capital managed by productive HH
  - $q_t$  = price of physical capital
  - $p_t$  = price of money
  - $f_t$  = fee for intermediation (spread)  
as a function of the **state variable**  $\eta_t = N_t/K_t$
- Mechanic application of Ito's lemma – equilibrium conditions get transformed into ordinary differential equations for  $\pi(\eta)$ ,  $q(\eta)$ ,  $p(\eta)$  and  $f(\eta)$

# Equilibrium: p and q



# Observations

As  $\eta$  goes up:

- Intermediaries take on more risk, competition increases and fees for intermediation services go down
- Capital is allocated more efficiently, more productively
- The price of capital increases due to higher demand  $\Rightarrow$  greater productive efficiency
- Unproductive agents hold more inside money (deposits in financial institutions) and less outside fiat money
- The price of fiat money goes down (so it would go up in the event that  $\eta$  falls, leading to deflation)
- There is an additional source of amplification relative to an economy without money: as  $\eta$  goes down, the value of assets fall, while the value of liabilities increase (due to deflation)

# || Roadmap

- Big picture overview
- Passive monetary policy: “Gold standard”
  - Model setup
  - 2 polar cases
    - Impaired i-sector “lending” via outside money only
    - Perfect i-sector perfect lending
  - General model with aggregate risk
    - Lending and money multiplier depends on net worth of i-sector
    - Deflation spiral
- Active Monetary Policy
  - Introduce long-term bond
    - Short-term interest rate policy
    - Asset purchase and OMO
  - Redistributive effects
  - “Greenspan put” - Time-inconsistency

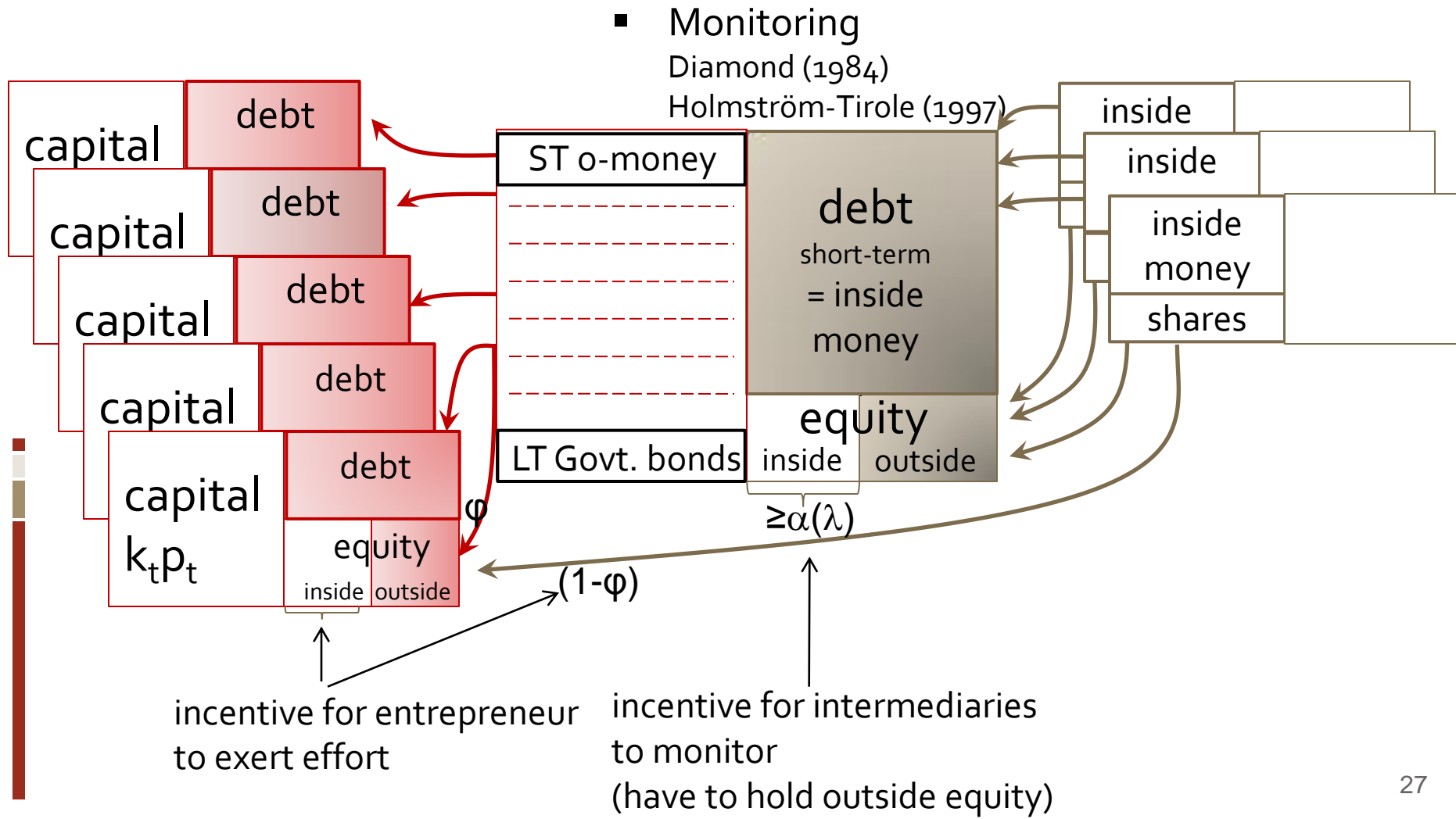
# Monetary policy

So far, outside money fixed, pays no interest (“Gold standard”)  
+ no central bank

- Short-term interest rate policy
  - Central bank accepts deposits & pays interest (by printing money)
    - E.g. short-term interest rate is lowered when  $\eta$  becomes small
  - Introduce consol (perpetual) bond
    - pays interest rate in ST (outside) money
  - Budget neutral policies
- Asset purchases
  - Bond – open market operations (OMO)
  - Outside equity
  - Risky capital  $k_t$
- Perfect commitment (Ramsey) vs. imperfect commitment
  - Markovian (in  $\eta$ )

# Instrument 1: short-term interest rate

- Productive
- Intermediary
- Less productive



# Instrument 1: short-term interest rate

- Without long maturity assets changes in short-term interest rate has no effect
  - Interest rate change equals instantaneous inflation change
- With long-term bond  
(monetary instruments: fraction  $\chi$  is cash and  $1 - \chi$  are bonds)
- with bonds, deflationary spiral is less pronounced because as  $\eta$  goes down, growing demand for money is absorbed by increase in value of long-term bonds



# Instrument 2: Asset purchase (OMO)

- Open market operation
  - changes “maturity structure of government obligations”
  - Redistributes wealth if monetary policy is accommodative
  - Intuition:
    - As  $\eta$  declines  $i(\eta)$  is lowered. This increases the value of G-bonds which helps to stabilize  $\eta$ .
    - For low  $\eta$  maturity structure of overall o-money rises
    - (Monetary policy should depend on maturity structure of government debt)
- Aside: short-term interest rate changes often also involve very small scale OMO

# Optimality of monetary policy

- Lowers risk on liability side of intermediaries

$$(\sigma_t^q + \sigma - \sigma_t^p - \kappa_t \sigma)$$



- Signal = fundamental risk + valuation risk + money risk
  - Signal precision increases
  - Improves “incentives”



# || Moral hazard – “Liquidity bubbles”

- Accommodating Monetary policy rule
  - “Greenspan put”
    - Ex-post efficient – recapitalizes intermediary sector
    - Ex-ante inefficient – if excessive stimulates risk taking on behalf of intermediaries “Liquidity bubble”
- Time consistency problem with
  - Intermediaries/bankers instead of workers/labor unions
- Rationale for banking regulation
  - To reduce probability of low  $\eta$  realizations

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- Differences to New Keynesian framework

	New Keynesian	I-Theory
Key friction	Price stickiness	Financial friction
Driver	Demand driven as firms are obliged to meet demand at sticky price	Misallocation of funds increases incentive problems and restrains firms/banks from exploiting their potential
Monetary policy <ul style="list-style-type: none"> <li>• First order effects</li> </ul>	Affect HH's intertemporal trade-off Nominal interest rate impact real interest rate due to price stickiness	Ex-post: redistributinal effects between financial and non-financial sector  Ex-ante: insurance effect leading to moral hazard in risk taking (bubbles) - Greenspan put -
<ul style="list-style-type: none"> <li>• Second order effects</li> </ul>	Redistributinal between firms which could (not) adjust price	
Time consistency	Wage stickiness Price stickiness + monopolistic competition	Moral hazard

	New Keynesian	I-Theory
Risk build-up phase		Endogenous due to accommodating monetary policy
Net worth dynamics	zero profit → no dynamics	dynamic
State variables	Many exogenous shocks Intermediation/friction shock	Endogenous intermediation shock
Monetary policy rule	Taylor rule (is approximately optimal only if difference in $u'$ is well proxied by output gap) <ul style="list-style-type: none"> <li>• spreads</li> <li>• credit aggregates (?)</li> </ul>	Depends on signal quality and timeliness of various observables
Policy instrument	Short-term interest rate + expectations	Short-term interest rate + <b>long-term bond</b> + expectations
Role of money	In utility function (no deflation spiral)	Storage Precautionary savings

# Conclusions/further research

- Unified macromodel to analyze both
  - Financial stability                      2<sup>nd</sup> pillar of the ECB
  - Monetary stability                      1<sup>st</sup> pillar
    - Liquidity spirals
    - Fisher deflation spiral
- Capitalization of banking sector is key state variable
  - Price stickiness plays no role (unlike in New Keynesian models)
- Monetary policy rule
  - Redistributive feature
  - Time inconsistency problem – “Greenspan put”
- Future research
  - Persistent productivity shocks
  - Maturity mismatch in intermediary sector